Rational Expressions

- 1. For each question determine:
 - a) the values of x for which the rational expression is equal to 0
 - b) the values of x for which the expression is undefined

1.
$$\frac{(x-3)(x+2)}{(x-6)(x+1)}$$
 2. $\frac{2x^2+3x+1}{x^2-9}$ 3. $\frac{x^2-25}{x^2+8x+15}$

2. Simplify the following expressions

1.
$$\frac{25x^3y^2}{15xy^4}$$
 2. $\frac{3x^2 - 27}{4x - 12}$ 3. $\frac{x^2 - 6x - 27}{x^2 - 2x - 15}$

4.
$$\frac{3x^2 - 10x + 8}{3x^2 - x - 4}$$
 5.
$$\frac{2x^2 + 11x + 12}{x^3 + x^2 - 12x}$$

3. Multiplication and division

$$1. \frac{3x^3}{2y^2} \cdot \frac{8y^4}{27x^2} \qquad 2. \left(\frac{16x^3y^2}{25ab^5}\right) + \left(\frac{24xy^3}{15a^3b^2}\right) \qquad 3. \frac{x^2 - 16}{x^2} \cdot \frac{x^2 - 4x}{x^2 - x - 12}$$

4.
$$\frac{x^2 - 2x - 35}{2x^3 - 3x^2} \cdot \frac{4x^3 - 9x}{7x - 49}$$

5.
$$\frac{x^2 - 16}{x^2 - 10x + 25} + \frac{3x - 12}{x^2 - 3x - 10}$$

6.
$$\frac{x^3 + 4x}{x^2 - 16} + \frac{x^2 + 8x + 15}{x^2 + x - 20}$$

7.
$$\frac{x^2 - 36}{x^2 - 8x + 16} + \frac{3x - 18}{x^2 - x - 12}$$

4. Addition and subtraction

1.
$$\frac{3+x}{x} + \frac{4}{x}$$

2. $\frac{2x^2+5x-9}{x-5} + \frac{x^2-19x+4}{x-5}$
3. $\frac{x-2}{x+3} + \frac{x+2}{x-4}$
4. $\frac{x^2}{x-5} + \frac{25}{5-x}$
5. $\frac{x-2}{4x+8} - \frac{x+6}{5x+10}$
6. $\frac{1}{2x} + \frac{5x}{x^2-1} + \frac{3}{x+1}$
7. $\frac{3x}{x^2-7x+10} - \frac{2x}{x^2-8x+15}$
8. $\frac{3x-2}{x^2+2x-24} - \frac{x-3}{x^2-16}$
9. $\frac{2}{x+3} - \frac{x}{x-1} + \frac{x^2+2}{x^2+2x-3}$
5. Solving Equations:

1.
$$\frac{2}{5} + \frac{t}{4} = 1$$

2. $\frac{x+1}{3} - \frac{x+2}{6} = \frac{x+5}{4}$
3. $\frac{x}{3} + \frac{x}{4} = \frac{7}{2}$
4. $\frac{4}{x-5} + \frac{3}{x+5} = \frac{40}{x^2-25}$
5. $\frac{5}{x-10} + \frac{2}{x-4} = \frac{9}{x^2-14x+40}$
6. $\frac{5x}{x+1} + \frac{4}{x} = 9$